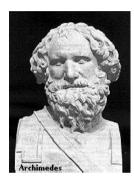
Física dos Meios Contínuos

Margarida Telo da Gama Rodrigo Coelho

History

Faces of Fluid Mechanics



Archimedes (C. 287-212 BC)



Navier (1785-1836)



Newton (1642-1727)



Stokes (1819-1903)



Leibniz (1646-1716)



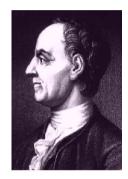
Reynolds (1842-1912)



Bernoulli (1667-1748)



Prandtl (1875-1953)



Euler (1707-1783)



Taylor (1886-1975) 2

Significance

• Fluids everywhere

Weather & climate

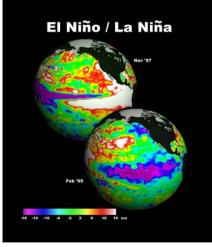
- Vehicles: automobiles, trains, ships, and planes, etc.
- Environment
- Physiology and medicine
- Sports & recreation
- O Many other examples!

Weather & Climate

Tornadoes



Global Climate



Thunderstorm



Hurricanes



Vehicles

Aircraft



High-speed rail



Surface ships



Submarines



Environment

Air pollution



River hydraulics



Physiology and Medicine

Blood pump

Ventricular assist device



A BVS blood pump



Sports & Recreation

Water sports



Cycling



Offshore racing



Auto racing



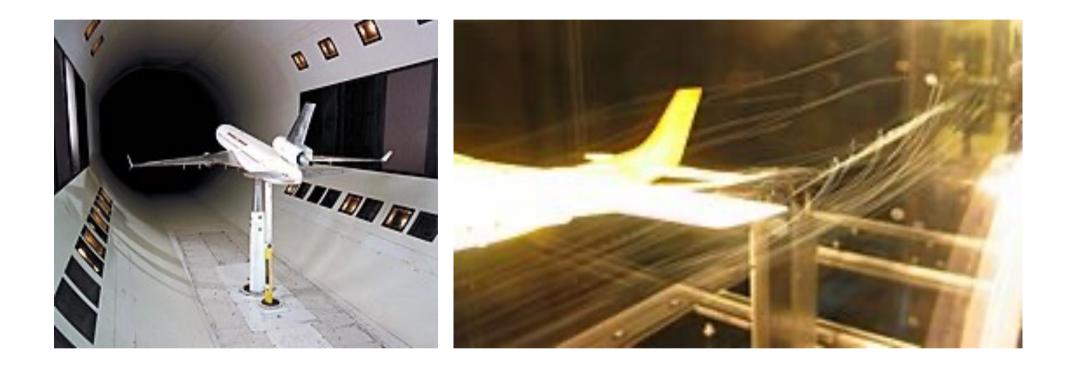
Surfing



Analytical Fluid Dynamics

- Mathematical physics problem formulation
- Control volume & differential analysis (RTT)
- Exact solutions exist ONLY for simple geometry and conditions
- Approximate solutions for practical applications
 - Linear
 - Empirical relations using EFD data

Full and model scales: wind tunnel



- Scales: full-scale and model
- Selection of the model scale: governed by dimensional analysis and similarity

Computational Fluid Dynamics

- CFD is use of computational methods for solving fluid engineering systems, including modeling (Mathematics & Physics) and numerical methods (solvers, finite differences, grid generations, etc.).
- Rapid growth in CFD technology since advent of computer





IBM WorkStation

Purpose

- The objective of CFD is to model the continuous fluids with Partial Differential Equations (PDEs) and discretize PDEs into an algebra problem, solve it, validate it and achieve simulation based design instead of "build & test"
- Simulation of physical fluid phenomena that are difficult to be measured by experiments: scale simulations (full-scale ships, airplanes), hazards (explosions, radiations, pollution), physics (weather prediction, planetary boundary layer, stellar evolution).

Modeling

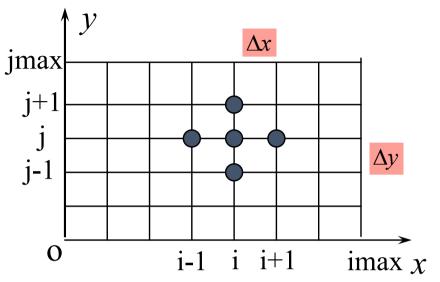
- Mathematical physics problem formulation of fluid engineering system
- Governing equations: Navier-Stokes equations (momentum), continuity equation, energy equation, ideal gas law, combustions (chemical reaction equation), multi-phase flows and turbulent models (RANS, LES, DES)
- Coordinates: Cartesian, cylindrical and spherical coordinates result in different forms of governing equations
- Initial conditions (initial guess of the solution) and Boundary Conditions (no-slip wall, free-surface, zero-gradient, symmetry, velocity/pressure inlet/outlet)
- Flow conditions: Geometry approximation, domain, Reynolds Number, and Mach Number, etc.

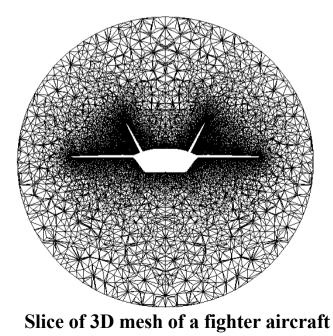
Numerical methods

• Finite difference methods: using numerical scheme to approximate the exact derivatives in the PDEs

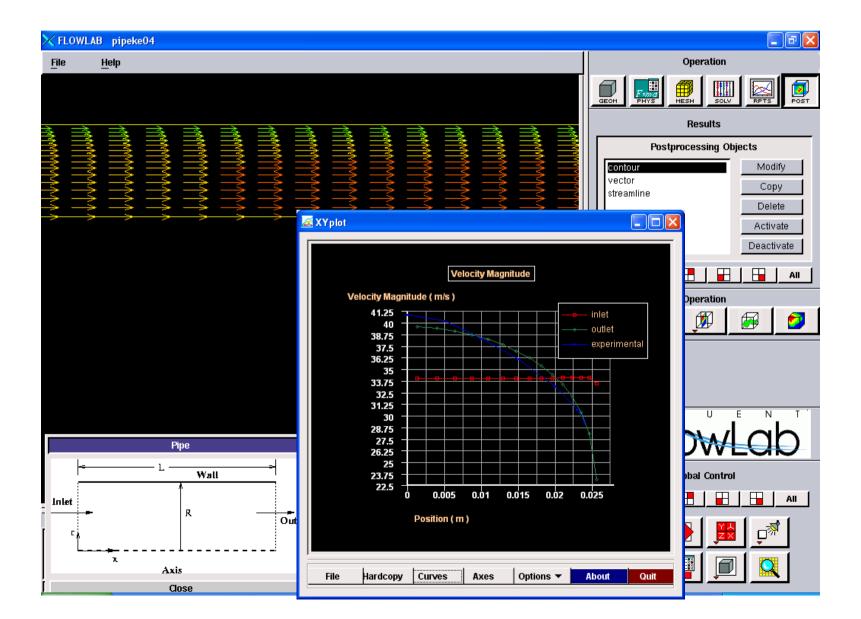
$$\frac{\partial^2 P}{\partial x^2} = \frac{P_{i+1} - 2P_i + P_{i-1}}{\Delta x^2}$$
$$\frac{\partial^2 P}{\partial y^2} = \frac{P_{j+1} - 2P_j + P_{j-1}}{\Delta y^2}$$

- Finite volume methods
- Grid generation: conformal mapping, algebraic methods and differential equation methods
- Grid types: structured, unstructured
- Solvers: direct methods (Cramer's rule, Gauss elimination, LU decomposition) and iterative methods (Jacobi, Gauss-Seidel, SOR)

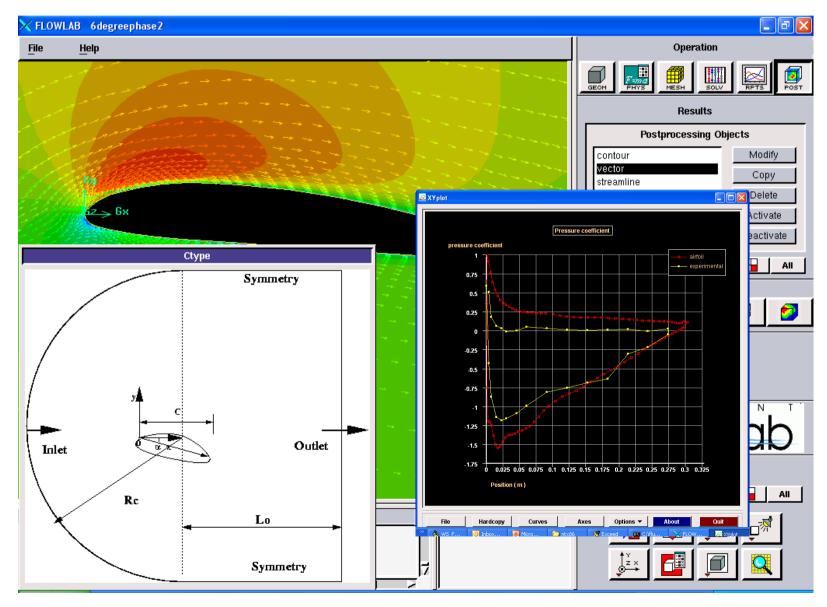




"Hands-on" experience using CFD Interface (pipe template)



"Hands-on" experience using CFD Interface (airfoil template)



Designing, building and operating a submarine

